

Estimate of intense rainfall equation parameters for rainfall stations of the Paraíba State, Brazil¹

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ABSTRACT

Rainfall is the primary water source for hydrographic basins. Hence, the quantification and knowledge of its temporal and spatial distribution are indispensable in dimensioning hydraulic projects. This study aimed at assessing the fit of a series of rainfall data to different probability models, as well as estimating parameters of the intensity-duration-frequency (IDF) equation for rain stations of the Paraíba State, Brazil. The rainfall data of each station were obtained from the Brazilian Water Agency databanks. To estimate the maximum daily rainfall of each station and return period (5, 10, 15, 25, 50 and 100 years), the following probability distributions were used: Gumbel, Log-Normal II, Log-Normal III, Pearson III and Log-Pearson III. The estimation of rainfall in durations of 5-1,440 min was carried out by daily rainfall disaggregation. The adjustment of the IDF equation was performed via nonlinear multiple regression, using the nonlinear generalized reduced gradient interaction method. When compared to the data observed, the intense rainfall equations for most stations showed goodness of fit with coefficients of determination above 0.99, which supports the methodology applied in this study.

KEYWORDS: Hydrology; intensity-duration-frequency equation; rainfall.

INTRODUCTION

Water is a natural resource with a wide range of uses and is vital to the human development. Maintaining this finite resource at adequate standards of quality and quantity for its multiple uses is a challenge to society. Rainfall is the primary source of water for hydrographic basins. As such, its quantification and the knowledge of how it is temporally and spatially

RESUMO

Estimativa de parâmetros das equações de chuvas intensas para estações pluviométricas do Estado da Paraíba, Brasil

As chuvas constituem-se na principal fonte de água para bacias hidrográficas. Por isso, a quantificação e o conhecimento de sua distribuição temporal e espacial são indispensáveis para o dimensionamento de projetos hidráulicos. Objetivou-se avaliar a aderência de séries de dados pluviométricos a diferentes modelos probabilísticos e estimar parâmetros da equação de intensidade-duração-frequência (IDF) para estações pluviométricas do Estado da Paraíba. Os dados pluviométricos de cada estação foram obtidos a partir do banco de dados da Agência Nacional de Águas. Para estimar as precipitações máximas diárias de cada estação e o período de retorno (5, 10, 15, 25, 50 e 100 anos), foram utilizadas as seguintes distribuições de probabilidade: Gumbel, Log-Normal II, Log-Normal III, Pearson III e Log-Pearson III. A estimativa das chuvas nas durações de 5-1.440 min foi realizada pela desagregação das precipitações pluviométricas diárias. O ajuste da equação IDF foi realizado por meio de regressão múltipla não linear, com uso do método de interação de gradação reduzida generalizada não linear. As equações de chuvas intensas para a maioria das estações, quando comparadas aos dados observados, apresentaram ajustes com coeficientes de determinação acima de 0,99, o que referenda a metodologia empregada neste trabalho.

PALAVRAS-CHAVE: Hidrologia; equação intensidade-duração-frequência; pluviosidade.

distributed are essential in studies related to irrigation needs, water availability for domestic and industrial uses, soil erosion, flood control and water projects, among others (Oliveira et al. 2005, Araújo et al. 2008, Santos et al. 2010, Castro et al. 2011).

According to Mello et al. (2008), the 21st century should experience a great frequency of extreme temperature and rainfall events. These maximum rainfalls, also denominated intense rainfalls

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(Silva et al. 2012, Souza et al. 2012, Aragão et al. 2013), produce a large volume of water in a short period of time. As such, they are apt to cause large surface flows and considerable damage in both urban and agricultural areas in the form of floods, dam ruptures, inundation of cultivated land, soil erosion, silting and contamination of water bodies (Cecílio et al. 2009, Santos et al. 2009). The knowledge of rainfall volume at a specific time and space is important for planning soil and water conservation practices and hydrographic basin management, in order to establish the flow used in different types of hydraulic projects (Back 2009, Cecílio et al. 2009, Santos et al. 2009).

To characterize rainfall, it is necessary to know its duration, intensity and frequency of occurrence. These relationships are commonly denominated intensity-duration-frequency (IDF) curves, one of the most widely used methodologies in rainfall-flow transformation processes (Damé et al. 2008). Intense rainfall is determined by empirical adjustments of IDF equation parameters, derived from rainfall data for each of the stations (Santos et al. 2009, Back et al. 2012). The parameters of the intense rainfall equation can be obtained via nonlinear multiple regression, based on information extracted from the series of rainfall data (Campos et al. 2014), which do not always contain duration, but are composed of daily records. However, it is necessary to know which rainfalls lasted less than 24 h, in order to adjust IDF equations (Aragão et al. 2013). One alternative is disaggregation based on proportionality factors, which makes possible to obtain rainfall duration in minutes (Cetesb 1986, Garcia et al. 2011, Aragão et al. 2013).

In the Brazilian Paraíba State, pioneering studies on intense rainfall were conducted by

Pfafstetter (1957), who used rainfall records from stations located in the cities of João Pessoa and São Gonçalo. For these areas, Pfafstetter (1957) adjusted the parameters of the relationship between rainfall and return period for different durations. In other study, Souza (1972) used data from João Pessoa to develop the IDF equation for this station. Since these outdated reports were the only ones available for Paraíba, a State that depends greatly on the efficient use of water for its cropping activities, it is required to update and estimate them for other locations in this region.

Due to the significant lack of information about rainfall intensity-duration-frequency (IDF) for most locations in Paraíba, and given the importance of knowing such information for the design of irrigation projects, this study aimed at estimating the parameters of the IDF equation for rainfall stations in this State.

MATERIAL AND METHODS

The study was carried out in 2014, at the Universidade Federal do Piauí, in Bom Jesus, Piauí State, Brazil. Daily rainfall data were collected from 132 stations in the Paraíba State, obtained from the Brazilian Water Agency databank (Brasil 2012).

First, the consistency of the data series of each station was analyzed, and those with less than 16 years of observation were excluded, leaving only one per municipality, and a total of ninety stations (Figure 1).

A series of mean maximum 1-day rainfalls was obtained for the following return periods: 5, 10, 15, 25, 50 and 100 years. The probability distributions

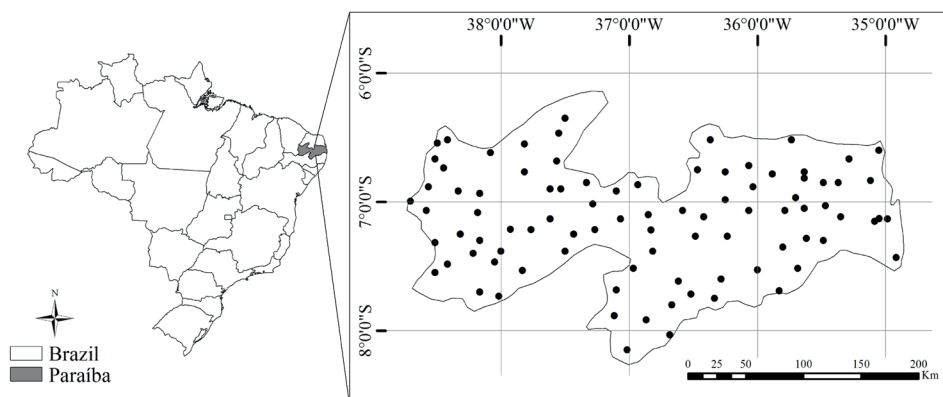


Figure 1. Location of ninety rainfall stations used to estimate the intensity-duration-frequency (IDF) equations for the Paraíba State. Source: Brasil (2012).

used were: Gumbel, Log-Normal II, Log-Normal III, Pearson III and Log-Pearson III (Santos 2010). For each station, the maximum rainfall in which the data series showed the best fit to the probability model was selected, i.e., the distribution model with the lowest standard error. All these stages were conducted using the SisCAH software (Sousa et al. 2009). Afterwards, the probability model that best fitted the data series was determined to estimate the maximum daily rainfall, and the number of occurrences of each model was counted.

Once the maximum daily rainfalls had been established, 1-day rainfall disaggregation was performed at 5, 10, 15, 20, 25, 30, 60, 360, 480, 600, 720 and 1440 min, using the coefficients from the rainfall disaggregation method proposed by Cetesb (1979) (Table 1).

Once the fit of distribution data to the probability model had been assessed and disaggregation was achieved at shorter times, the parameters K, a, b and c of the intensity-duration-frequency equation were established (Equation 1), according to Pfafstetter (1982):

$$M_i = \frac{K \cdot RP^a}{(t + b)^c} \quad (1)$$

where M_i is the mean maximum rainfall, in mm h^{-1} ; RP the return period, in years; t the rainfall duration, in min; and K, a, b, and c the parameters adjusted based on the rainfall data for the location.

The IDF equation parameters were adjusted via nonlinear multiple regression, using the generalized reduced gradient interaction method, and goodness of fit was assessed based on the coefficient of determination (r^2) estimated by the Equation 2:

$$r^2 = \left(\frac{\sum(x - \bar{x}) \cdot (y - \bar{y})}{\sqrt{\sum(x - \bar{x}) \cdot (y - \bar{y})}} \right)^2 \quad (2)$$

where x is the observed values; \bar{x} the observed mean values; y the estimated values; and \bar{y} the estimated mean values.

Goodness of fit was also evaluated using the regression equation of data observed in relation to the estimated data, considering, in this case, the angular coefficient of the straight line.

After the parameters (K, a, b and c) were adjusted, they were used to estimate the maximum rainfall intensity for the return period of 25 years, as well as duration of 5, 30, 60, 360, 720 and 1,440 min. Next, these data were regionalized for all the Paraíba State, using the kriging method and ArcGis 10 software.

RESULTS AND DISCUSSION

From the probability models that exhibited the best fit for the series of rainfall data, the highest standard error observed was 41.83. Considering the standard error values obtained, more than one of the probability models provided a good fit to a same data series, according to the return period. This indicates that the model that best fits each return period should be used to estimate the maximum rainfall in different return periods. Lyra et al. (2006) observed the goodness of fit of different probability models to estimate rains at different periods of the year, indicating that fitting models is directly linked to the temporal distribution of rainfall. This confirms the need to apply more than one probability model to analyses covering different times, providing a greater security to projects dimensioned according to these estimated rainfall values.

Of the ninety stations studied, the Log-Normal III model showed the best fit to the data series (49.3 % of the stations), followed by the Gumbel model, with 16.1 % of the stations. The models with the poorest fit were Pearson III, Log-Pearson III and Log-Normal II, with 14.1 %, 12.8 % and 7.8 % of the stations, respectively (Figure 2). Martins et al. (2011) estimated the maximum flow and rainfall using probability models, also obtaining a better fit with the Log-Normal III distribution model. These findings are similar to those reported by Silva et al. (2003a), in determining the parameters of IDF equations for the Tocantins State, Brazil. These results confirm that, in addition to the Gumbel model (Santos et al. 2009), widely recommended in literature, the Log-Normal III may also be useful to estimate rainfall

Table 1. Coefficients used for daily rainfall disaggregation in shorter time intervals.

Rainfall-flow transformation interval	Coefficient
1 day to 24 h	1.14
1 day to 12 h	0.85
24 h to 10 h	0.82
24 h to 8 h	0.78
24 h to 6 h	0.72
24 h to 1 h	0.42
1 h to 30 min	0.74
1 h to 25 min	0.91
1 h to 20 min	0.81
1 h to 15 min	0.70
1 h to 10 min	0.54
1 h to 5 min	0.34

Source: Cetesb (1979).

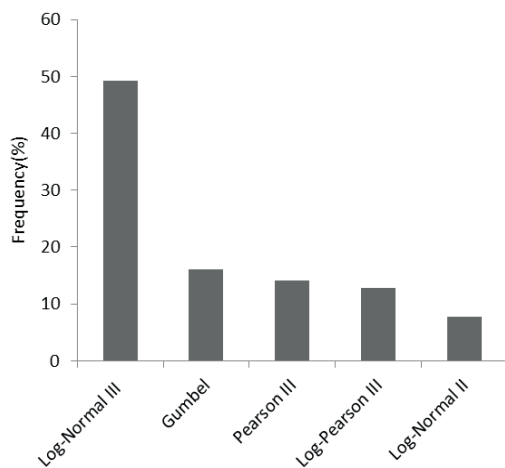


Figure 2. Frequency of the best fits to the respective probability distribution models.

in different return periods, having the lowest standard error of the estimates as a fit criterion.

The values of the fitting IDF parameters varied significantly from one station to another. The K parameter estimates ranged between 473.139 and 2095.776, respectively for the Remígio and Santa Rita stations. Moruzzi & Oliveira (2009), Souza et al. (2012) and Silva et al. (2012) also reported a similar variation for this parameter, attributing that to the interaction between K and the other IDF parameters. The estimates of the parameter “a” ranged between 0.025 and 0.386, respectively for the Sousa and Santa Rita stations; parameter “b” between 9.836 and 30.214, respectively for the Remígio and Santa Rita stations; and parameter “c” between 0.745 and 0.915, respectively for the Remígio and Santa Rita stations (Table 2). Similar

Table 2. Adjusted values for parameters of the intensity-duration-frequency (IDF) equation¹ and respective determination coefficient (r²) for each studied rainfall station in the Paraíba State, Brazil.

City	Code	K	a	b	c	r ²	City	Code	K	a	b	c	r ²
Água Branca	737022	1,070.08	0.110	13.110	0.780	0.999	Mogeirol	735010	807.748	0.199	13.511	0.783	0.998
Aguiar	738025	981.794	0.186	12.030	0.768	0.999	Monteiro	737014	623.267	0.258	11.114	0.759	0.998
Alagoa Grande	735033	1,141.473	0.187	18.694	0.829	0.992	Mulungu	735009	827.096	0.224	16.065	0.806	0.994
Alagoa Nova	735030	1,251.040	0.271	19.055	0.832	0.986	Nazarezinho	638048	1,068.721	0.187	13.129	0.779	0.999
Alhandra	734008	973.248	0.207	10.327	0.751	0.998	Nova Olinda	738014	1,240.531	0.178	13.314	0.781	0.998
Aracagi	635027	891.732	0.202	13.420	0.782	0.998	Olho D'água	737011	1,166.909	0.112	13.216	0.780	0.998
Araruna	635028	978.242	0.228	14.452	0.792	0.996	Olivedos	636036	1,170.203	0.289	18.511	0.828	0.987
Areia	635030	982.504	0.214	15.391	0.800	0.996	Passagem	737010	1,087.539	0.136	13.373	0.782	0.998
Aroeiras	735029	658.247	0.203	13.956	0.787	0.998	Patos	737009	1,134.552	0.173	15.045	0.797	0.996
Bananeiras	635033	912.592	0.169	13.581	0.783	0.998	Pedra Lavrada	636037	1,049.774	0.167	17.593	0.820	0.995
Barra de Santa Rosa	636032	483.566	0.256	10.806	0.756	0.999	Piancó	737006	1,053.249	0.164	13.421	0.782	0.998
Barra de São Miguel	736025	1,111.353	0.266	17.977	0.823	0.992	Picuí	636038	1,010.135	0.311	21.656	0.853	0.982
Boa Ventura	738012	1,172.065	0.083	12.633	0.774	0.999	Pilar	735035	756.675	0.245	10.795	0.756	0.999
Bonito de Santa Fé	738022	1,129.402	0.114	12.985	0.778	0.999	Pilões	638046	915.392	0.149	11.097	0.759	0.999
Boqueirão	735124	612.044	0.246	11.226	0.760	0.999	Pocinhos	736014	732.276	0.241	15.806	0.804	0.996
Brejo do Cruz	637023	1,143.916	0.265	18.479	0.827	0.989	Pombal	637032	896.259	0.138	12.121	0.769	0.999
Cabaceiras	736022	596.260	0.259	11.816	0.766	0.999	Prata	737004	1,144.219	0.132	13.172	0.780	0.998
Cachoeira dos Índios	638030	1,032.572	0.207	13.164	0.779	0.998	Princesa Isabel	738013	939.905	0.172	11.997	0.768	0.999
Cajazeiras	638028	981.336	0.134	11.635	0.764	0.999	Remígio	636031	473.139	0.272	9.836	0.745	0.998
Camalau	736021	1,274.816	0.150	12.913	0.777	0.998	Salgadinho	736010	713.824	0.234	11.402	0.762	0.999
Campina Grande	736024	801.209	0.253	15.254	0.799	0.995	Santa Luzia	636042	929.464	0.113	13.712	0.785	0.998
Catolé do Rocha	637030	1,003.170	0.125	12.540	0.773	0.995	Santa Rita	734001	2,095.776	0.386	30.214	0.915	0.957
Conceição	738020	1,147.336	0.227	16.158	0.807	0.994	Santa Teresinha	735036	992.153	0.179	11.849	0.767	0.999
Condado	637028	1,034.455	0.085	12.742	0.775	0.999	Santana dos Garrotes	738019	832.018	0.170	13.502	0.783	0.998
Congo	736018	1,139.564	0.185	16.556	0.811	0.995	São João do Cariri	736020	666.983	0.231	11.275	0.761	0.999
Coremas	737021	1,274.682	0.091	12.725	0.775	0.999	São João do Rio do Peixe	638032	937.692	0.135	11.175	0.760	0.999
Cruz do Espírito Santo	735019	995.833	0.140	12.676	0.775	0.998	São João do Tigre	836001	968.835	0.241	16.313	0.809	0.995
Cuité	636040	901.149	0.136	13.724	0.785	0.998	São João da Lagoa Tapada	638049	1,272.876	0.120	13.239	0.780	0.998
Desterro	637029	1,200.708	0.336	23.953	0.871	0.977	São João de Espinharas	637034	1,064.522	0.130	11.857	0.767	0.999
Fagundes	735018	942.259	0.134	13.327	0.781	0.998	São José de Piranhas	738024	972.242	0.140	11.514	0.763	1.000
Guarabira	635040	1,142.183	0.223	15.405	0.800	0.996	São José dos Cordeiros	736011	1,063.892	0.097	13.283	0.781	0.998
Gurjão	736016	1,296.963	0.160	14.184	0.789	0.997	São Mamede	637037	1,222.403	0.097	13.224	0.780	0.998
Ibiara	738018	1,267.511	0.147	13.472	0.782	0.998	São Sebastião do Umbuzeiro	837000	1,005.777	0.111	14.074	0.788	0.998
Imaculada	737017	824.171	0.172	11.411	0.762	0.999	Serra Branca	736017	1,132.579	0.147	14.479	0.792	0.997
Ingá	735017	649.214	0.213	12.741	0.775	0.999	Serra Grande	738010	1,033.868	0.167	12.047	0.768	0.999
Itaporanga	738017	1,052.685	0.158	12.929	0.777	0.999	Serraria	635048	865.400	0.148	13.414	0.782	0.998
Jacaraú	635043	1,002.352	0.119	13.658	0.784	0.998	Solânea	635047	861.431	0.146	13.988	0.787	0.997
Jericó	637036	1,337.724	0.073	12.889	0.777	0.999	Soledade	736006	869.831	0.142	13.792	0.786	0.998
Juazeirinho	736015	1,020.790	0.086	13.140	0.779	0.998	Sousa	638051	1,134.511	0.025	12.196	0.770	0.999
Juru	737016	950.321	0.142	11.729	0.765	0.999	Sumé	736026	1,121.638	0.158	14.136	0.789	0.997
Mãe D'água	737015	1,234.298	0.263	16.956	0.814	0.991	Taperoá	736000	887.501	0.141	11.684	0.765	0.999
Malta	637031	1,276.634	0.225	16.291	0.808	0.995	Teixeira	737002	1,141.531	0.137	14.285	0.790	0.997
Mamanguape	635044	1,220.824	0.222	15.030	0.797	0.997	Triunfo	638029	893.550	0.152	13.371	0.781	0.998
Manaira	738015	1,148.691	0.119	13.257	0.780	0.998	Uirauna	638035	1,017.264	0.031	12.503	0.773	0.999
Mataraca	635045	1,531.710	0.126	13.372	0.781	0.998	Umbuzeiro	735011	807.748	0.199	13.511	0.783	0.989

¹ The parameters K, a, b and c are defined by Pfafstetter (1982).

results have been reported in others studies, with the variability in IDF parameters attributed primarily to the different rainfall distribution (Silva et al. 2003b, Santos et al. 2009, Campos et al. 2014).

Silva et al. (2002) also found a wide variation in the estimates of the IDF equation parameters in a study carried out in the Bahia State. For the K parameter, the estimates ranged from 1121.260 to 8999.000; parameter “a” from 0.174 to 0.245; parameter “b” from 19.457 to 56.068; and parameter “c” from 0.783 to 1.119. Similarly, Santos et al. (2009) also observed a significant variation for stations assessed in the Mato Grosso do Sul State. These results confirm that the IDF of rainfall is directly linked to its spatial distribution (Silva et al.

2002, Santos. et al. 2010), corroborating the need to determine these parameters for each specific rainfall station.

In most of the equations adjusted by applying the daily rainfall disaggregation methodology, the r^2 values were above 0.99, and of the ninety stations studied, only three exhibited values below 0.99, the lowest being 0.97 at the Santa Rita station. These results show the good fit of the estimates obtained by the methodology used, in relation to the data observed.

The spatialization of maximum rainfall intensity values with the estimates of the IDF equation parameters shows that the greatest intensities, regardless of duration, occur in the coastal and highlands at the “sertão” of the Paraíba State (Figure 3).

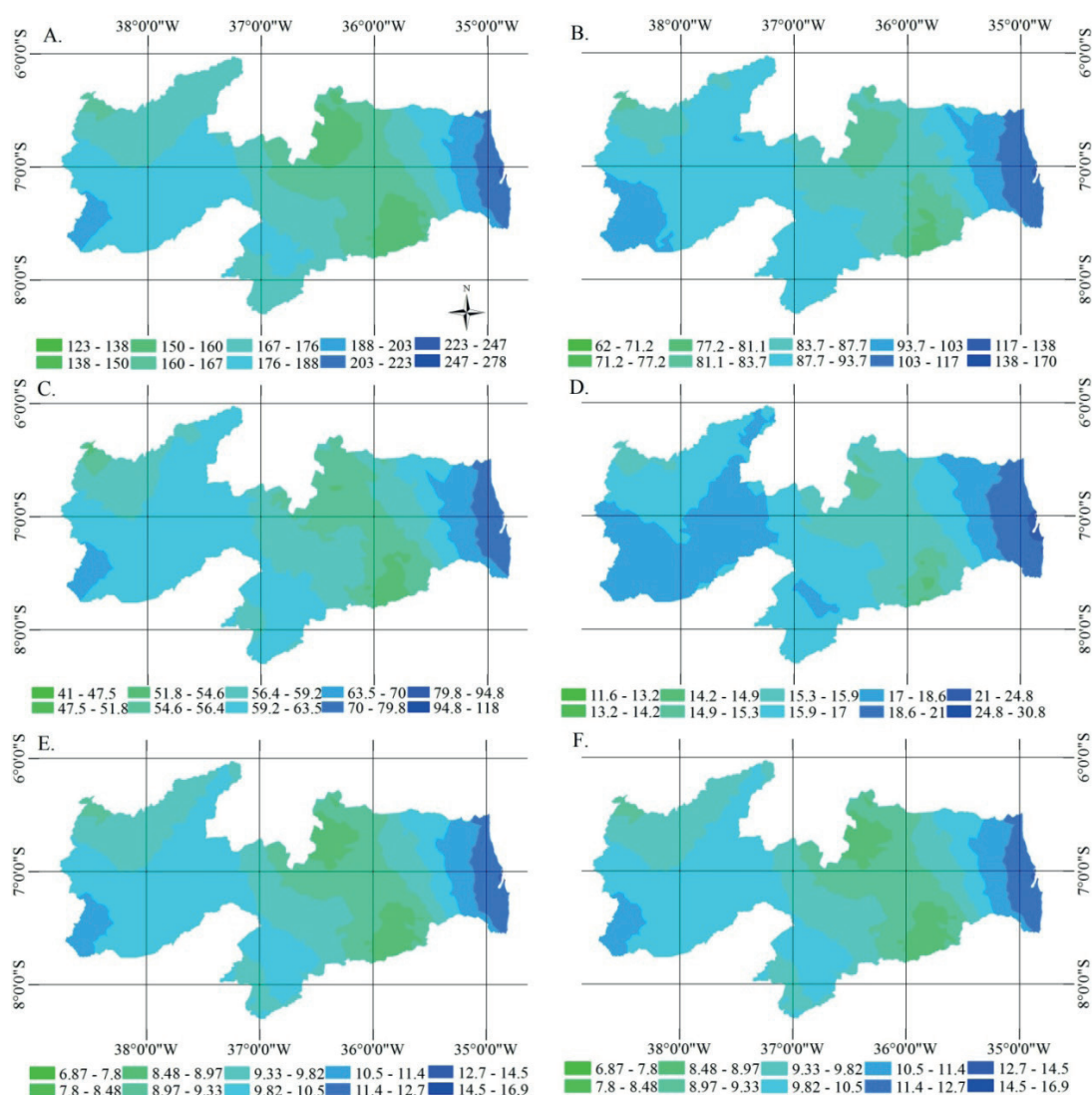


Figure 3. Maximum rainfall intensities (mm) estimated for a return period of 25 years, with the following durations: 5 min (A), 30 min (B), 60 min (C), 360 min (D), 720 min (E) and 1,440 min (F).

In general, the spatial distribution of maximum rainfall intensity estimated by the IDF equation corroborates other studies on rainfall pattern in the Paraíba State (Limeira et al. 2012, Silva et al. 2009). These findings demonstrate that the rainfall values estimated for different durations and return periods by IDF equations have a high correlation with the rainfall distribution observed in this region.

CONCLUSIONS

1. The Log-Normal III distribution model shows a better fit to the data series, for determination of maximum rainfalls for different return periods in the Paraíba State;
2. The intense rainfall equations for most stations showed a good fit, with coefficients of determination above 0.99, supporting the methodology used in this study;
3. The intensity-duration-frequency (IDF) equation parameters show a wide variation among stations, indicating the need to determine them for each station;
4. The spatialization of the maximum rainfall intensity values with the estimates of IDF equation parameters shows that the highest intensities occur in the regions of coastal and highlands at the “sertão” of the Paraíba State.

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