

# Adjustment of water-crop production models for ratoon sugarcane<sup>1</sup>

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## RESUMO

Ajuste de modelos de produção água-cultura para cana-soca

Modelos de produção precisam ser testados em diferentes locais, para serem utilizados como instrumento de planejamento agrícola. Avaliaram-se, ao longo de nove ciclos de cultivo, as relações hídricas e o desempenho de modelos de produção água-cultura, na estimativa da produtividade de cana-soca, em Paranavaí (PR). Estimou-se a evapotranspiração de referência e real da cultura, armazenamento de água no solo, deficiência e excedente hídrico. Os modelos de “Stewart” e “Jensen” obtiveram os melhores desempenhos para estimar a produtividade de cana-soca. A disponibilidade hídrica na primeira fase de desenvolvimento da cana-soca exerce a maior influência na produtividade.

**PALAVRAS-CHAVE:** *Saccharum* spp.; evapotranspiração; relações hídricas.

## ABSTRACT

Production models need to be tested at different locations to be used as an agricultural planning tool. Hydric relations and performances of water-crop production models were used to estimate ratoon sugarcane yield along nine production cycles, in Paranavaí, Paraná State, Brazil. The crop reference and real evapotranspiration, soil water storage, water deficit and surplus were evaluated. The “Stewart” and “Jensen” models showed the best performance to estimate ratoon sugarcane yield. Water availability in the first development phase of ratoon sugarcane has the greatest influence on yield.

**KEY-WORDS:** *Saccharum* spp.; evapotranspiration; water relations.

## INTRODUCTION

Sugarcane (*Saccharum* spp.) is one of the main products in the Brazilian agribusiness. In the Paraná State, sugarcane occupies an area of 665,000 ha, with an annual production of about 50 million tons. The Paranavaí region accounts for 20 % of this production, and the planted area is increasing fast in this region (Paraná 2015).

Agriculture is the economic activity that has a higher dependence on weather conditions, which are responsible for the oscillations of agricultural seasons (Souza 2014). Environmental factors directly affect plant growth and development. However, the relations between climatic parameters and agricultural production are quite complex. The influence of climate on sugarcane is remarkable because it is a semi-perennial crop, grown under different environmental conditions, causing production variations over the years (Silva et al. 2008).

The effect of water stress on sugarcane, at different development phases, is not well defined, making it difficult to estimate how the lack or excess of soil moisture affects yield (Wiedenfeld 2000). However, it is known that the damage promoted by stress depends on which developmental phase the plant is and the stress duration. The longer the period with low water availability, the greater the damage on stalks and saccharose yield (Inman-Bamber 2004, Farias et al. 2008).

In sugarcane management, it is always important to forecast the production, given the changes occurring in soil and climate throughout the cropping season (Silva & Bergamasco 2001). Detailed knowledge on water dynamics in the soil-water-atmosphere system provides essential elements for the establishment or improvement of agricultural management practices aimed at optimizing yield (Souza 2014).

For a better understanding of plant-climate interaction, water-crop models have been used

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to characterize the effects of temperature and precipitation variations on crop yield (Frizzzone et al. 2005). Season forecasts from simulation models and other estimates can be successfully used in various situations to rationalize management practices (Souza 2013, 2014).

The use of water-crop models can have applications prior to sowing and during crop growth and development (Hoogenboom 2000). The information obtained may be used for planting planning and agricultural management, to improve the knowledge on the crop physiological mechanisms, minimize environmental risks, reduce production costs and provide greater sustainability in agricultural planning. However, for a model to be used under different conditions from those in which it was developed, it is necessary that their parameters be locally tested and adjusted, since its application depends on the obtained results (Araújo et al. 2011, Souza et al. 2013).

This study aimed at evaluating the water relations and the performance of simplified functions (linear, potential, exponential and logarithmic) and water-crop models to estimate ratoon sugarcane yield, in soil and climate conditions of Paranavaí.

## MATERIAL AND METHODS

The RB72454 cultivar, with an average cycle of 365 days, was used. Ratoon sugarcane yield data were collected for nine production cycles, in the 1997/1998 and 2007/2008 cropping seasons. In every season, the harvest was carried out in July, with equal length of days after sowing.

Data were collected at the Experimental Station of the Universidade Federal do Paraná, in Paranavaí, Paraná State, Brazil (22°58'44"S, 52°27'51"W and average altitude of 480 m). The

site has a medium texture Oxisol and mildly hilly topography (Silva et al. 2005). The soil physical attributes showed textural uniformity in depth. The soil is very permeable, homogeneous and without impediment layers (Table 1).

Stalks were distributed in plant lines (grooves) arranged with 18 internodes per linear meter, spaced 1.40 m between rows. Soil chemical properties were evaluated before the sugarcane planting at every cycle. The base fertilizer used was 20 kg ha<sup>-1</sup> of N, 100 kg ha<sup>-1</sup> of K<sub>2</sub>O and 100 kg ha<sup>-1</sup> of P<sub>2</sub>O<sub>5</sub>. Harvests were performed manually and cultural practices were carried out according to the standard management for sugarcane in the region.

The sugarcane yield was estimated using four simplified functions (linear, potential, logarithmic and exponential) and six water-crop models specific for the Paranavaí region. Regression and correlation analyses with four simplified functions were used to verify the adjustment of real yield, with the following water component data: reference evapotranspiration (*ET<sub>0</sub>*), crop evapotranspiration (*ET<sub>c</sub>*), real evapotranspiration (*ET<sub>r</sub>*), *ET<sub>r</sub>/ET<sub>c</sub>* and precipitation.

Following recommendations of Frizzzone et al. (2005), the water-crop models bellow were used to estimate yield:

$$\text{- Howell \& Hiler (1975): } \frac{Y_r}{Y_p} = \frac{\sum_{i=1}^n (ET_r)_i}{\sum_{i=1}^n (ET_c)_i}$$

$$\text{- Jensen (1968): } \frac{Y_r}{Y_p} = \prod_{i=1}^n \left( \frac{ET_r}{ET_c} \right)_i^{\lambda_i}$$

$$\text{- Minhas et al. (1974): } \frac{Y_r}{Y_p} = \prod_{i=1}^n \left[ 1 - \left( 1 - \frac{ET_r}{ET_c} \right)_i^2 \right]^{\lambda_i}$$

Table 1. Texture (sand, silt and clay), specific soil mass ( $\rho$ ) and volumetric moisture content at field capacity ( $\theta_{FC}$ ) and permanent wilting point ( $\theta_{PWP}$ ) averages, in the 1997/1998 and 2007/2008 cropping seasons, at different depths (Paranavaí, Paraná State, Brazil).

Depth	Sand	Silt	Clay	$\rho$	$\theta_{FC}$	$\theta_{PWP}$
	%			kg m <sup>-3</sup>	m <sup>3</sup> m <sup>-3</sup>	
0-20 cm	83.3	1.1	15.5	1,640	0.10	0.06
20-40 cm	82.9	1.0	16.0	1,610	0.22	0.07
40-60 cm	84.1	1.3	14.5	1,620	0.21	0.07
60-80 cm*	84.1	1.3	14.5	1,620	0.21	0.07

\* Estimated parameters.

$$\text{-Doorenbos \& Kassam (1979): } \frac{Y_r}{Y_p} = 1 - \left[ k_y \cdot \left( 1 - \frac{ET_r}{ET_c} \right) \right]$$

$$\text{- Stewart et al. (1976): } \frac{Y_r}{Y_p} = 1 - \left[ \sum_{i=1}^n k_{y_i} \cdot \left( 1 - \frac{ET_r}{ET_c} \right)_i \right]$$

$$\text{- Rao et al. (1988): } \frac{Y_r}{Y_p} = \prod_{i=1}^n \left[ 1 - k_{y_i} \cdot \left( 1 - \frac{ET_r}{ET_c} \right)_i \right]$$

where  $Y_r$ : sugarcane estimated yield ( $\text{kg ha}^{-1}$ );  $Y_p$ : sugarcane potential yield in the region ( $\text{kg ha}^{-1}$ );  $ET_r$ : real evapotranspiration at the  $i$ -th development phase ( $\text{mm cycle}^{-1}$ );  $ET_c$ : crop evapotranspiration at the  $i$ -th development phase ( $\text{mm cycle}^{-1}$ );  $k_y$  or  $k_{y_i}$ : penalty coefficient of yield by deficit for the different sugarcane development phases (dimensionless);  $\lambda_i$ : water factor penalty of yield by deficit for the different sugarcane development phases (dimensionless);  $i$ : crop development phases;  $n$ : number of development phases.

The sugarcane development phases and duration of the sub-periods were adapted from Machado et al. (1982), Sinclair et al. (2004) and Silva et al. (2005) (Table 2). The rooting system effective depth was defined according to Ido et al. (2006) and the crop coefficient values ( $kc$ ) used to transform  $ET_o$  in  $ET_c$  were adjusted for the period based on the figures provided by Doorenbos & Kassam (1979).

To obtain the main parameters and coefficients required in the water-crop models, potential yield ( $Y_p$ ) was considered the highest yield achieved during the period analyzed for the RB72454 cultivar, in the experiment site. The experimental data provided by PMGCA/UFPR/RIDESA (2008) indicated an average yield of  $154.19 \text{ t ha}^{-1}$ , in the 2005/2006 season.

The estimated yield analyzes with water-crop models were performed using coefficients or penalty factors for the different phases of sugarcane

development. These coefficients and factors were obtained from: (a) the literature, i.e., with no adjustment; (b)  $k_{y_i}$  coefficients and  $\lambda_i$  factors adjusted with simple ( $k_y$ ) and multiple ( $k_{y_i}$  e  $\lambda_i$ ) linear regression analyses (Souza 2014). These adjustments were made to the sugarcane relative yield ( $Y/Y_m$ ) and relative evapotranspiration ( $ET_r/ET_c$ ) using climatic and cropping data from the nine studied cropping seasons. The regressions were resolved with the minimum square method and the linear equations system with the Gaussian elimination method (Souza 2013).

Yield estimates for each season were made from the integration of water-crop models, in a spreadsheet containing: a) the penalty factors and yield coefficients by deficit for the different sugarcane development phases (available in literature or adjusted); b)  $ET_c$  and  $ET_r$  values obtained in the calculation of daily water balance, in each  $i$ -th sugarcane development phase and  $j$ -th season, in the Paranavaí region.

The accuracy of the estimate of each water-crop model was determined from the linear regression analysis and correlation between the annual values of real and estimated yield (raised in the region). The agreement index “ $d$ ” of Willmot et al. (1985) and the index “ $c$ ” of Camargo & Sentelhas (1997) were used to assess the degree of accuracy between actual and estimated sugarcane yield values.

The estimated components of water balance were obtained according to Thornthwaite & Mather (1955). Precipitation and other climatic data required to estimate the daily reference evapotranspiration ( $ET_o$ ) were provided by the Paraná Meteorological System, from an automatic meteorological station. The  $ET_o$  estimation was performed using the Penman-Monteith method (Allen et al. 1998).

The determination of soil physical properties (texture, density and moisture content at field capacity and permanent wilting point) was needed to

Table 2. Ratoon sugarcane development phases, rooting system effective depth ( $Z$ ) and crop coefficient ( $kc$ ) (Paranavaí, Paraná State, Brazil).

Development phase	Start	End	Duration	$Z$	$kc$
			days	m	dimensionless
I	July	October	93	0.60	0.40
II	October	March	160	0.80	1.25
III	March	July	112	0.80	0.75

Source: adapted from Machado et al. (1982), Sinclair et al. (2004) and Silva et al. (2005). I: sprouting to intense tillering; II: growth in height; III: reduction of growth and sucrose accumulation.

allow the calculation of soil available water capacity (*AWC*). Disturbed and undisturbed soil samples were collected in the experimental area, at eight collecting points, subdivided into three depths (0-0.20 m, 0.20-0.40 m and 0.40-0.60 m). The volumetric ring method (Embrapa 1997) was used to determine the density and points of the soil water retention curve. The parameters of the Van Genuchten (1980) equation were estimated with the Splintex software, version 1.0 (Prevedello 1999). The moisture content at field capacity and permanent wilting point were determined considering the tensions of 0.0098 MPa and 1.470 MPa, respectively.

*AWC* was determined by the following equation:  $AWC_i = 0.01 \cdot (\theta_{FC} - \theta_{PWP}) \cdot z_i$ , where  $AWC_i$ : soil available water capacity in the *i*-th development phase (mm);  $\theta_{FC}$ : volumetric soil moisture at field capacity (%);  $\theta_{PWP}$ : volumetric soil moisture at the wilting point (%);  $z_i$ : effective depth of root system in the *i*-th crop development phase (mm).

Allen et al. (1998) present typical values of available water fraction (*p*) to different crops, indicating 0.65 for sugarcane, with which it was possible to calculate the soil available water (*SAW*). The cosine equation was used to determine the soil water storage and/or “negative accumulated” (Rijtema & Aboukhaled 1975).

## RESULTS AND DISCUSSION

The yield in the 2007/2008 season was 16.04 % lower than the average yield of the region (80 t ha<sup>-1</sup>).

This was the only season that had yield below the regional average. The low performance observed occurred because the 2007/2008 season had the lowest values of *ETr*, precipitation and surplus, and the highest deficit (Table 3). Except for the 1999/2000 and 2007/2008 seasons, the precipitation values were always higher than the crop evapotranspiration (*ETc*) values. This fact caused high water surplus values, when considering the whole year, but did not prevent the occurrence of water deficit in specific periods, like during the growing season.

In the development phase I (budding to intense tillering), the average water deficit was 15.2 mm. Although Inman-Bamber & Smith (2005) say that sugarcane has resilience to moderate water stress during phase I, yield decreased mainly in 1998/1999 and 2007/2008, when the water deficit was more intense (Table 3). The water deficit occurred mainly in the development phase II (growth in height), possibly due to the fast crop development (Table 4). In phase II, plants have large leaf area and require a lot of water for gas exchange with the atmosphere (Ramesh 2000). In the development phase III (decreased growth and sucrose accumulation), the average deficiency was 41.4 mm. Data from phase III showed that water stress causes losses in sucrose production (Inman-Bamber & Smith 2005).

Obtaining models from commonly used functions (linear, potential, exponential and logarithmic), from simple regression analysis, when possible, is an excellent way to estimate a given

Table 3. Water balance components and average yield for ratoon sugarcane, from the 1997/1998 to the 2007/2008 season (Paranavai, Paraná State, Brazil).

Season	<i>ETo</i>	<i>ETc</i>	<i>ETr</i>	Precipitation	Deficit	Surplus	<i>ETr/ETc</i>	Yield <sup>(1)</sup> t ha <sup>-1</sup>
	mm season <sup>-1</sup>							
1997/1998	1,279.5	1,180.0	1,067.3	1,625.0	112.7	551.6	0.90	130.60
1998/1999	1,235.3	1,174.0	1,020.6	1,492.6	153.5	443.0	0.87	130.16
1999/2000	1,442.5	1,320.0	913.7	1,251.6	406.3	341.1	0.69	98.99
2000/2001	1,268.0	1,198.6	1,068.3	1,659.0	130.4	586.9	0.89	140.83
2001/2002	1,387.6	1,270.6	1,043.2	1,439.0	227.5	464.2	0.82	127.94
2002/2003	1,330.9	1,233.7	1,056.5	1,479.2	177.2	408.6	0.86	115.79
2003/2004	1,327.8	1,250.5	962.0	1,508.8	288.4	500.3	0.77	141.60
2005/2006	1,294.6	1,203.9	951.0	1,373.8	252.9	433.1	0.79	154.19
2007/2008	1,363.4	1,252.6	791.9	1,003.6	460.7	147.6	0.63	67.92
Mean	1,325.5	1,231.5	986.1	1,425.8	245.5	430.7	0.80	123.11
<i>S</i> <sup>(2)</sup>	64.74	47.40	91.87	188.49	114.70	121.93	0.09	26.06
CV (%) <sup>(3)</sup>	4.90	3.80	9.30	13.20	46.70	28.30	10.90	21.20

<sup>(1)</sup> Source: PMGCA/UFPR/RIDESA (2008); <sup>(2)</sup> standard deviation; <sup>(3)</sup> coefficient of variation. *ETo*: reference evapotranspiration; *ETc*: crop evapotranspiration; *ETr*: real evapotranspiration.

phenomenon based on an independent variable. However, the attempt to adjust the yield data of the nine seasons of sugarcane with climatic parameters ( $ET_o$ ,  $ET_c$ ,  $ET_r$ ,  $ET_r/ET_c$  and precipitation) had no significant effect. The best coefficient of determination ( $R^2$ ) obtained was less than 0.32.

The next attempt consisted in evaluating water-crop models using coefficients recommended in the literature (Table 5), which improved yield estimates, when compared with linear, potential, logarithmic and exponential functions. However, the analysis did not render any model with “very good” or “excellent” fit (Table 6).

Another procedure recommended to improve the accuracy of estimated yield with models consisted of performing the statistical adjustment of coefficients or factors, with data from the nine studied seasons, with simple or multiple regression analysis. With statistical adjustment, the coefficients or factors ( $k_y$ ,  $k_{y_i}$  and  $\lambda$ ) found with the tested models were close and similar to those recommended in the literature (Table 5), especially for the  $k_y$  obtained by regression with the Stewart et al. (1976) model proposed by Doorenbos & Kassam (1979). The similarity between the coefficients or factors statistically adjusted and recommended in the literature (determined in other

Table 4. Average components (seasons 1997/1998 to 2007/2008) of water balance in the different development phases of ratoon sugarcane (Paranavaí, Paraná State, Brazil).

Development phase	$AWC$	$ET_o$	$ET_c$	Precipitation	$ET_r$	Deficit	Surplus
	mm	mm phase <sup>-1</sup>					
I	65.3	318.7	127.5	270.6	112.3	15.2	146.7
II	93.9	697.2	871.2	753.7	627.9	243.3	144.4
III	93.9	325.8	244.4	308.8	203.0	41.4	103.7

$AWC$ : available water capacity;  $ET_o$ : reference evapotranspiration;  $ET_c$ : crop evapotranspiration;  $ET_r$ : real evapotranspiration.

Table 5. Coefficients and/or factors ( $k_y$ ,  $k_{y_i}$  and  $\lambda$ ) of water-crop models recommended in the literature and statistically adjusted for ratoon sugarcane (Paranavaí, Paraná State, Brazil).

Coefficient or factor	Phases			All cycle	Source
	I	II	III		
Recommended in literature					
$\lambda$	0.43	0.39	0.07	-	Jensen (1968)
$k_y$	0.75	0.50	0.10	-	Doorenbos & Kassam (1979)
Total $k_y$	-	-	-	1.20	Doorenbos & Kassam (1979)
Statistically adjusted in single or multiple regression with the season data					
$\lambda$	0.95	0.31	0.17	-	Multiple regression - Jensen (1968)
$\lambda$	1.91	1.55	0.90	-	Multiple regression - Minhas et al. (1974)
$k_y$	0.82	0.36	0.15	-	Multiple regression
Total $k_y$	-	-	-	0.92	Simple regression

Table 6. Coefficients of determination ( $R^2$ ) and index “ $d$ ” and “ $c$ ” of the performance obtained in the analysis comparing real and estimated yield with water-crop models, for ratoon sugarcane, using the literature (L) and adjusted (A) coefficients (Paranavaí, Paraná State, Brazil).

Model	$R^2$		Index “ $d$ ”		Index “ $c$ ”	
	L	A	L	A	L (Classification)	A (Classification)
Howell & Hiller (1975)	0.49	0.49	0.65	0.76	0.46 (“bad”)	0.53 (“tolerable”)
Minhas et al. (1974)	0.75	0.74	0.52	0.92	0.45 (“bad”)	0.79 (“very good”)
Stewart et al. (1976) proposed by Doorenbos & Kassam (1979)	0.78	0.81	0.78	0.95	0.69 (“good”)	0.86 (“optimum”)
Doorenbos & Kassam (1979)	0.49	0.49	0.68	0.73	0.48 (“bad”)	0.51 (“tolerable”)
Rao et al. (1988)	0.77	0.80	0.77	0.93	0.68 (“good”)	0.83 (“very good”)
Jensen (1968)	0.75	0.81	0.74	0.95	0.64 (“median”)	0.86 (“optimum”)

regions and conditions) shows that the tested water-crop models are meaningful and can potentially be applied to a broader region. Although many variables are involved in the sugarcane yield, water is considered one of the main factors. This is the reason that makes the coefficients and factors of water-crop models so similar, even when adjusted in different environments.

The analyses comparing real *versus* estimated yield values, using statistically adjusted coefficients with data from the nine seasons, improved the models to estimate ratoon sugarcane yield in Paranavaí (Table 6). Visually, it was found that the six models tested were sensitive to fluctuations of yield, even for models with a “c” index, classified as “poorly” (Howell & Hiler 1975, Doorenbos & Kassam 1979) (Figure 1).

The Stewart et al. (1976) model proposed by Doorenbos & Kassam (1979), as well as the Jensen (1968) model, showed a better performance (Table 6) and enabled yield estimates with an average error of 6.72 % and 6.79 %, respectively (Figure 1). These models are product operator type (i.e., multiplicative), in which the adverse effects occurring in a given development phase impact the results of the remaining phases. The good performance obtained with these multiplicative models indicate that ratoon sugarcane may indeed behave like that. Conversely, the other evaluated models assume that the crop behave in a similar way independently of the water restrictions occurring on previous development phases, what is not true.

Sensitivity analyzes conducted with the Jensen (1968) model demonstrated that the occurrence of

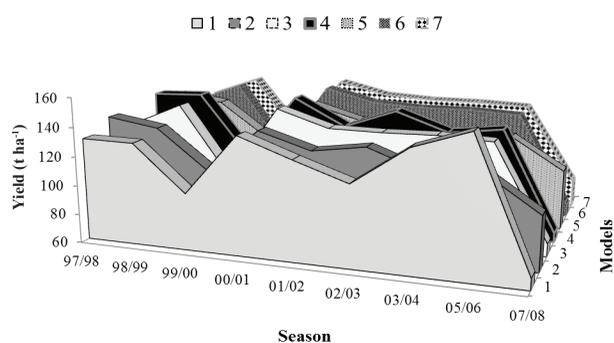


Figure 1. Real and estimated ratoon sugarcane yield from the 1997/1998 to the 2007/2008 season (Paranavaí, Paraná State, Brazil). 1 - Real yield; 2-7 - Estimated yield with models; 2 - Howell & Hiler (1975); 3 - Jensen (1968); 4 - Minhas et al. (1974); 5 - Doorenbos & Kassam (1979); 6 - Stewart et al. (1976) proposed by Doorenbos & Kassam (1979); 7 - Rao et al. (1988).

$ET_r/ETc_i$  ratio lower than 1.0 (deficit  $> 0$ ), for the  $i$ -th phases, resulted in yield loss, and can reach null values if the ratio is close to zero. Plants were less sensitive in the development phase III, for which low values of the  $ET_r/ETc_i$  ratio impacted less the sugarcane yield (Figure 2).

According to Embrapa (2009), an  $ET_r/ETc_i$  ratio higher than 0.6, in the  $i$ -th development phases, is sufficient to provide an adequate development to sugarcane and to achieve good yield levels. However, the Jensen (1968) model indicates that when the  $ET_r/ETc_i$  ratio reaches 0.6 in a single development phase, significant yield loss is predicted. The loss magnitude depended on the development phase in which the water deficit occurred. Values of  $ET_r/ETc_i$  equal to 0.6 occurred in the development phase I and resulted in a 38.3 % yield loss, in relation to the potential yield (154.19 t ha<sup>-1</sup>). For the development phases II and III, yield losses were 14.7 % and 8.2 %, respectively, in relation to the potential yield.

Variation in the  $ET_r/ETc$  ratio, in the development phase III, impacted yield the least. This result is in agreement with Inman-Bamber & Smith (2005), who concluded that the early development phases of sugarcane are the most susceptible to water deficit. They also observed that deficiencies occurring in the development phase III might contribute to sucrose accumulation.

The estimated sugarcane yield based on the Jensen (1968) model, with  $ET_r/ETc_i$  ratio fixed in 0.6 (WRSI considered satisfactory), in the three developmental phases, is 74.4 t ha<sup>-1</sup>. The value is 52.0 % lower than the potential yield (154.19 t ha<sup>-1</sup>), indicating that sugarcane is sensitive to water stress.

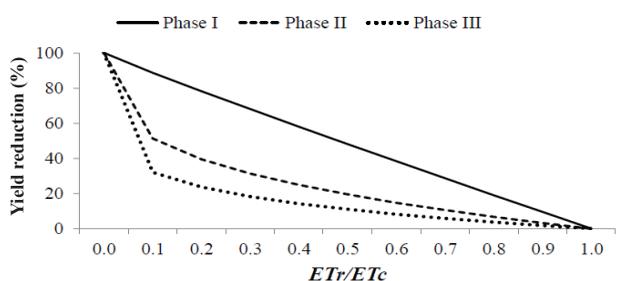


Figure 2. Yield reduction as a function of the  $ET_r/ETc$  ratio, based on the Jensen (1968) model, using statistically adjusted coefficients in the development phases I, II and III (Paranavaí, Paraná State, Brazil).

## CONCLUSIONS

1. Water-crop models using yield coefficients or penalty factors “recommended in the literature” did not have a good performance to estimate ratoon sugarcane yield.
2. The “Stewart” and “Jensen” models reached the best performance, with index classified as “great”, to estimate ratoon sugarcane yield.
3. Water availability in the first development phase of ratoon sugarcane influences yield more than in the other two phases.

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